

Probability Examples Related to Combinations

Data Science and A.I. Lecture Series

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$$\binom{26}{1} \times \binom{13}{1} = 26 \times 13 = 338 \Rightarrow P = \frac{338}{1326}$$

Example: Arranging Letters in STATISTICS

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- Probability:

$$P = \frac{\frac{8!}{3! \cdot 2!}}{\frac{10!}{3! \cdot 3! \cdot 2!}} = \frac{8! \cdot 3!}{10!} = \frac{6}{15} = \frac{2}{5}$$

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- Probability:

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