Covariance Simplified: Learn It Once, Understand It Forever!

Data Science and A.I. Lecture Series

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Definition of Covariance

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  - Provide insights into the relationship between X and Y.

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