

Understanding Probability: Sample Space, Sample Points, and Events

Data Science and A.I. Lecture Series

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 - For tossing two coins, $n(S) = 4$.

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- In complex experiments, each sample point corresponds to a unique combination of outcomes.

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- **Certain Event:** Contains all sample points in S .
 - Example: Rolling a die and getting any number from 1 to 6, $E = \{1, 2, 3, 4, 5, 6\}$.

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