Calculating Variance of Discrete Frequency Distribution Data Science and A.I. Lecture Series

Bindeshwar Singh Kushwaha

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Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
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f_i	2	1	1	1	1	1
$f_i x_i$						

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>					

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>				

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>			

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>		

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$						

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²				

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²			

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	$9a^{2}$	$16a^{2}$		

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f_i	2	1	1	1	1	1
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$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	$9a^{2}$	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

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f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

	Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
ſ	f _i	2	1	1	1	1	1
ſ	$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
	$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance =
$$\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$$

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

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$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

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Variance =
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$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
fi	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	$9a^{2}$	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Expanding this:

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance =
$$\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$$

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

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fi	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	$9a^{2}$	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Expanding this:

$$160 = \frac{92a^2}{7} - \frac{484a^2}{49}$$

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance =
$$\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$$

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

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$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance =
$$\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$$

Substituting the known values:

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

Expanding this:

$$160 = \frac{92a^2}{7} - \frac{484a^2}{49}$$

Combining the terms

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

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Substituting the known values:

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

Expanding this:

$$160 = \frac{92a^2}{7} - \frac{484a^2}{49}$$

Combining the terms

$$160 = \frac{644a^2 - 484a^2}{49}$$

	Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
	f_i	2	1	1	1	1	1
	$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
ĺ	$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance =
$$\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$$

Substituting the known values:

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

Expanding this:

$$160 = \frac{92a^2}{7} - \frac{484a^2}{49}$$

Combining the terms

$$160 = \frac{644a^2 - 484a^2}{49}$$

Thus

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance =
$$\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$$

Substituting the known values:

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

Expanding this:

$$160 = \frac{92a^2}{7} - \frac{484a^2}{49}$$

Combining the terms

$$160 = \frac{644a^2 - 484a^2}{49}$$

Thus

$$160 = \frac{160a^2}{49}, a = \sqrt{49} = 7$$

Xi	а	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
f_i	2	1	1	1	1	1
$f_i x_i$	2 <i>a</i>	2 <i>a</i>	3 <i>a</i>	4 <i>a</i>	5 <i>a</i>	6 <i>a</i>
$f_i x_i^2$	$2a^{2}$	4 <i>a</i> ²	9 <i>a</i> ²	$16a^{2}$	25 <i>a</i> ²	36 <i>a</i> ²

Let us calculate the following

$$N = \sum f_i = 7, \sum f_i x_i = 22a, \quad \sum f_i x_i^2 = 92a^2$$

Variance formula

Variance = $\frac{1}{N} \sum f_i x_i^2 - \left(\frac{1}{N} \sum f_i x_i\right)^2$

Substituting the known values:

$$160 = \frac{1}{7} \times 92a^2 - \left(\frac{22a}{7}\right)^2$$

Expanding this:

$$160 = \frac{92a^2}{7} - \frac{484a^2}{49}$$

Combining the terms

$$160 = \frac{644a^2 - 484a^2}{49}$$

Thus

$$160 = \frac{160a^2}{49}, a = \sqrt{49} = 7$$

Result

a=7